

# The Impact of Allocation Bias in Rare Disease Clinical Trials with Multiple Endpoints

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## ● Challenges in Rare Disease Trials:

- ▶ Drugs and treatments often lack approval or rely on low levels of evidence.
- ▶ Defining a **single primary endpoint** is difficult due to:
  - \* Heterogeneous clinical presentations.
  - \* Multiple phenotypes.
  - \* Individualized patient experiences with the disease.
  - \* Limited understanding of the disease's natural history.

## ● Advantages of Using Multiple Endpoints:

- ▶ Capture diverse aspects of the disease.
- ▶ Provide comprehensive information from the trial.
- ▶ Offer a holistic view of treatment effects.
- ▶ Address patient-specific needs, such as patient-centered outcome measures (PCOMs).



## Types of Multiple Endpoints

- **Multiple Primary Endpoints:** Each endpoint is evaluated independently, and demonstrating a treatment effect for at least one endpoint indicates efficacy.
- **Co-primary Endpoints:** Requires treatment effects to be demonstrated for all primary endpoints to conclude overall efficacy.
- **Multi-component Endpoints:** Combines multiple outcomes within a subject into a single score or rating that can be either weighted or unweighted, i.e. PCOMs.
- **Composite Endpoints:** Merges several endpoints into a single variable, such as the time-to-first occurrence of a set of events.



## Key Objective

Enhance the design and analysis strategies of rare disease clinical trials with multi-component endpoints to improve robustness and validity by mitigating allocation bias.

## Research Questions

How we can account for allocation bias during the planning and analysis phase of a clinical trial?



- **What is Allocation Bias?**

Allocation bias is caused by weaknesses in the allocation process of treatment assignment. For example, a lack of concealment or blinding can make the next treatment predictable, allowing the enrollment of certain patients to be denied and more favorable patients to be allocated to preferred treatments.

- **Regulatory Guidelines:**

- ▶ EMA (ICH E9) highlights the importance of addressing bias when interpreting treatment effects and comparisons.

- **Key Requirement:** Addressing allocation bias during the planning, implementation, and evaluation phases ensures trial validity.



# Randomization Procedures

- CR** Allocation accomplished by a fair coin toss
- EBC(p)** Patients are assigned with a probability equal to a biased coin toss that favors the group with less frequent allocations with probability  $p \geq 0.5$
- BSD(b)** Allocation with CR until a maximum tolerated imbalance  $b$ , then deterministic assignment to the group with fewer patients
- CHEN(p,b)** Patients are assigned with EBC(p) until a maximum imbalance  $b$ , then deterministic allocation to the group with fewer assignments
- MP(b)** Assignments by a randomization list which is uniformly selected from the subset of randomization lists generated by CR that keeps the maximum tolerated imbalance  $b$
- RAR** The method randomly assigns half of patients to the treatment or control group.
- PBR(k)** Patients are allocated in blocks of length  $k$ . Within these blocks, the allocation is according to RAR

(Rosenberger,2002)



The biasing policy quantifies allocation bias effects in clinical trials with multi-component endpoints.

## Key Assumptions

- Researcher knows previous, but not future treatment assignments.
- Researcher favors the experimental group.
- Better responders have higher expected scores in each endpoint component.
- Classification of responders as good, neutral, or worse responders.
- Researcher follows the Blackwell and Hodges convergence strategy (1957), and assigns the next patient to the group with fewer prior allocations.



**Biased Recruitment Process:** The researcher assigns the next patient to the group with fewer prior allocations:

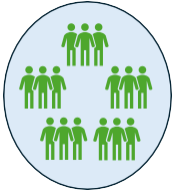
- **Experimental Group (E):** A good responder with increased expected response is recruited.
- **Control Group (C):** A worse responder with decreased expected response is selected.
- **Balanced Allocation:** A neutral responders are assigned.



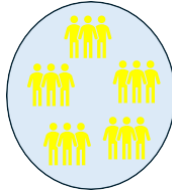


# Allocation Bias Policy

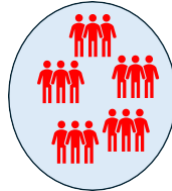
Good Responders



Neutral Responders



Worse Responders

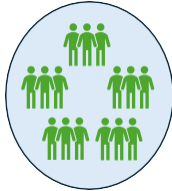


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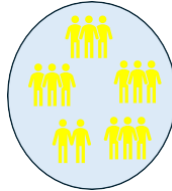
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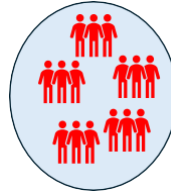
Good Responders



Neutral Responders



Worse Responders

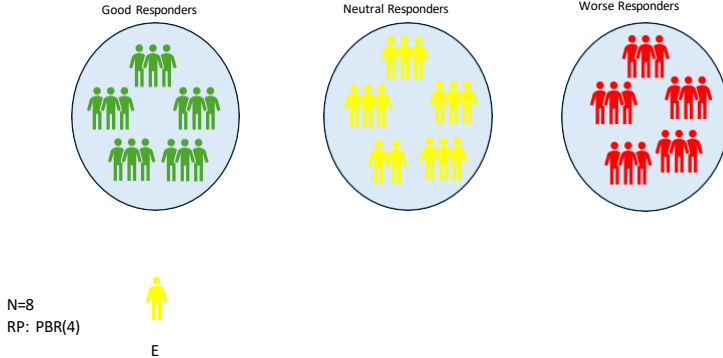


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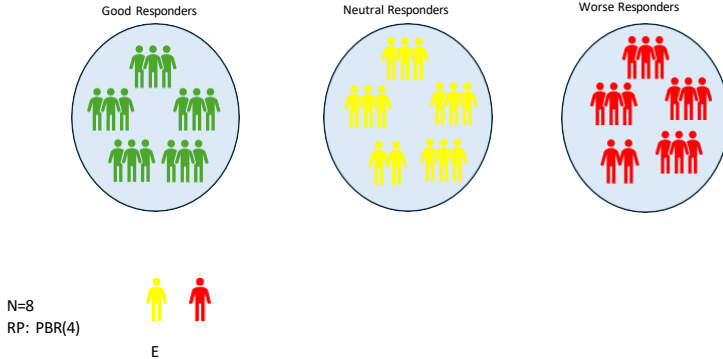
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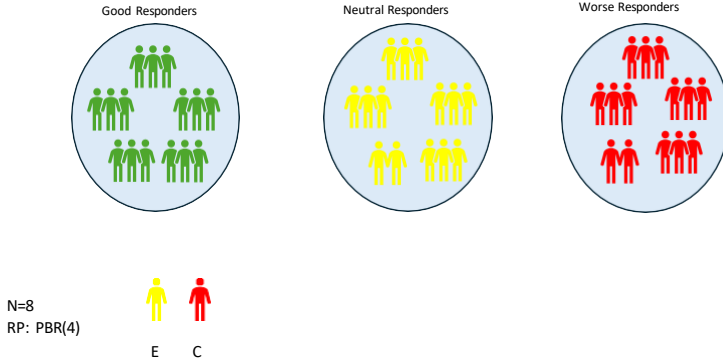
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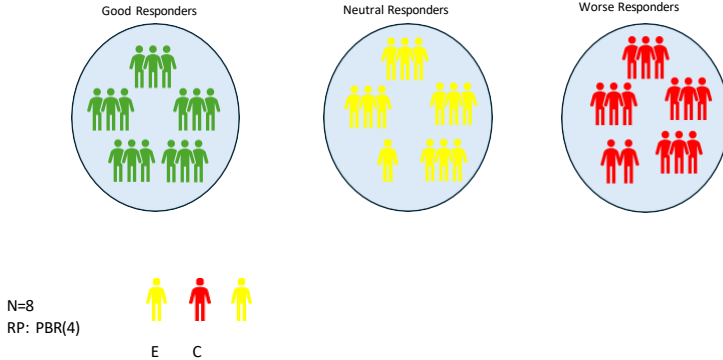
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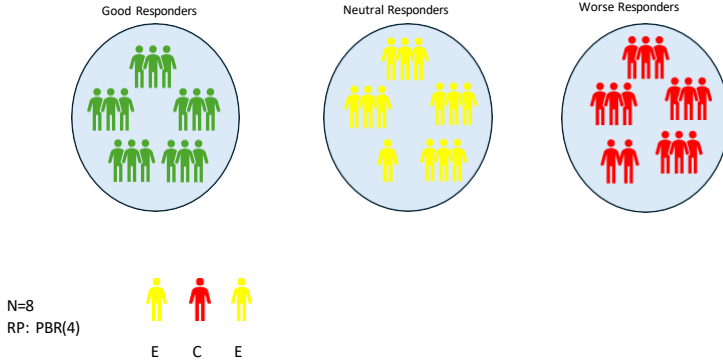
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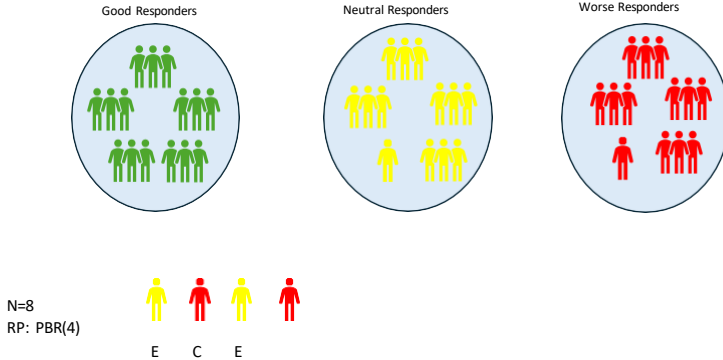
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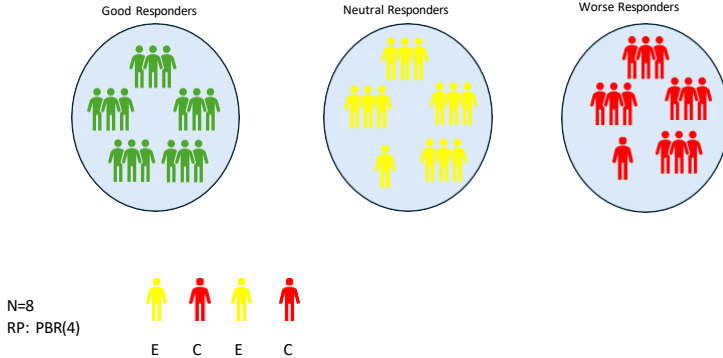


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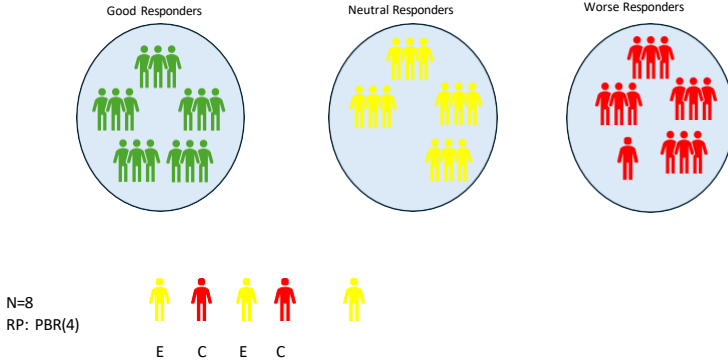




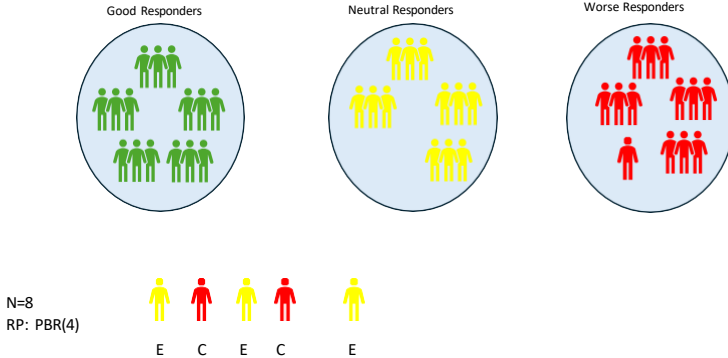
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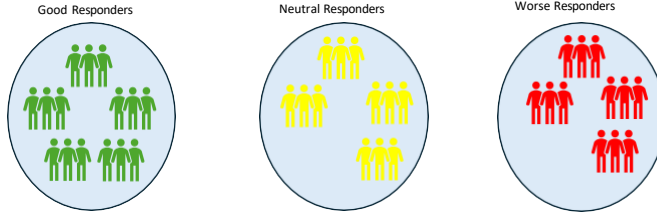
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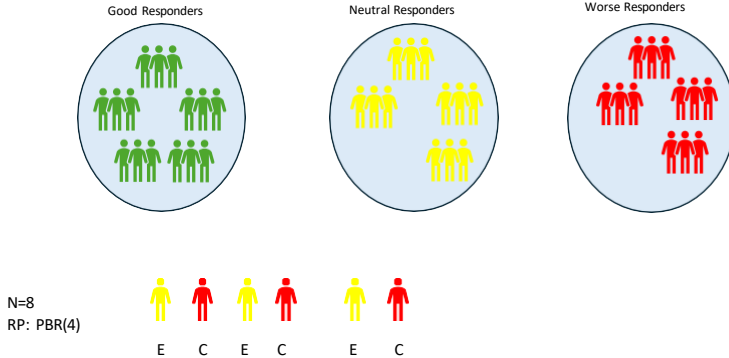
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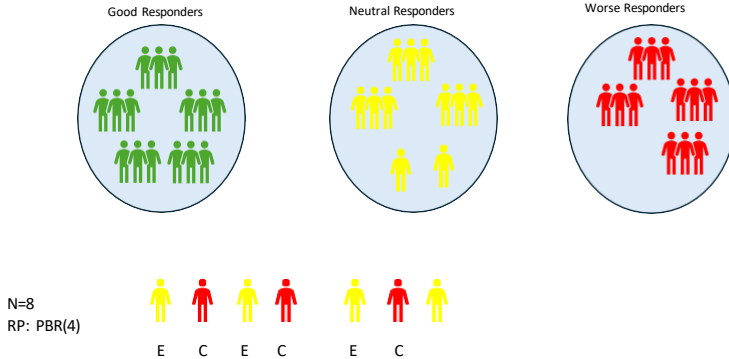
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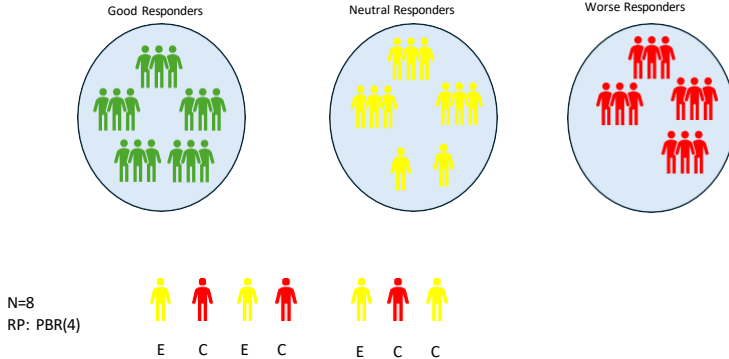
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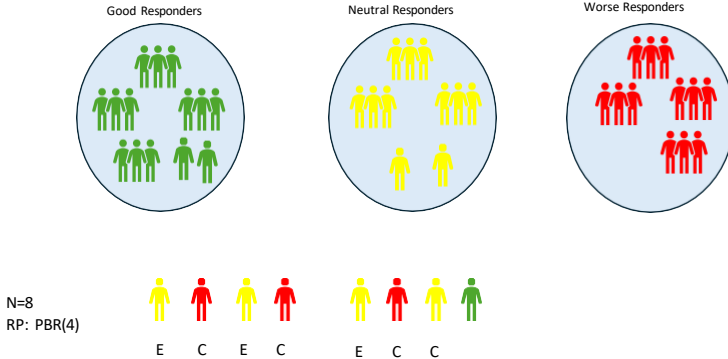
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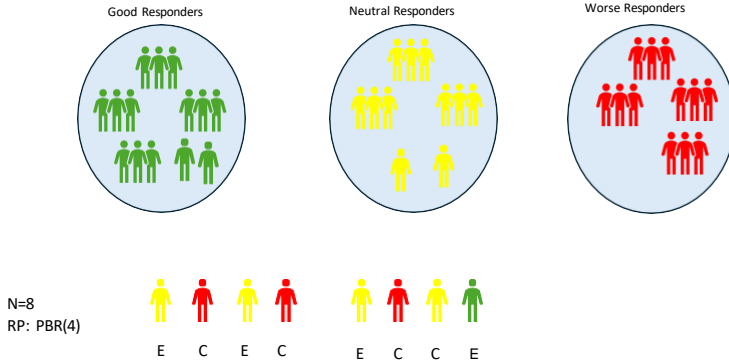


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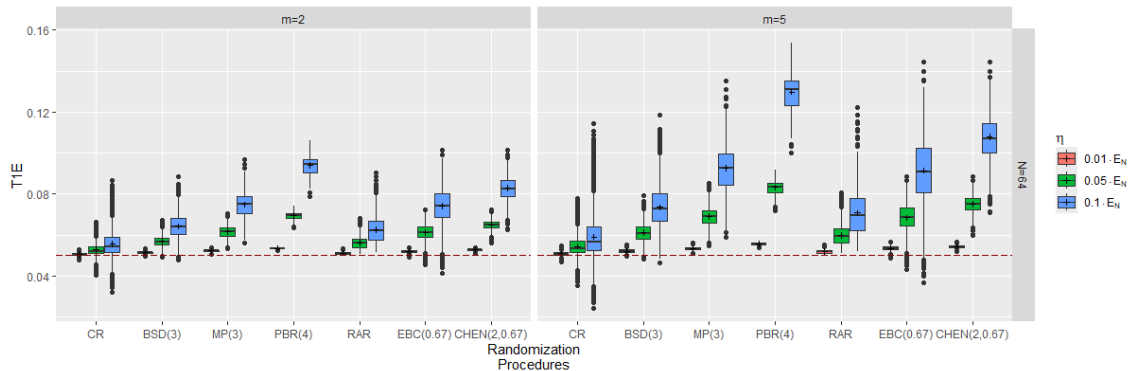


# Allocation Bias Policy



# Impact of Allocation Bias Policy

Simulation of **type I errors** (T1Es) of the **scoring test** when ignoring the presence of allocation bias, conditioned on 10 000 randomization lists, under homogeneous allocation bias effects of 1%, 5%, and 10% of the effect size  $E_N$ .



- **Impact of Allocation Bias:** Allocation bias inflates T1Es, potentially distorting trial results.
- **Role of Randomization Procedure:**
  - ▶ The extent of T1E inflation depends on the randomization method used.
  - ▶ **Best Performance:** Complete Randomization (CR) and Big Stick Design (BSD(3)).
  - ▶ **Worst Performance:** Permuted Block Randomization (PBR(4)).
  - ▶ Relaxing the final balance between treatment and control groups reduces bias.
- **Effect of Endpoint Components:** Increasing the number of endpoint components amplifies T1E inflation due to more components may introduce bias.



# Conclusion and Perspectives

- The allocation bias policy can be used to optimize clinical trials through:
  - ▶ Identifying the best randomization procedure that reduces allocation bias.
  - ▶ Validating trial results by performing bias-adjusted tests.

This approach ensures a more accurate assessment of treatment effects and enhances the validity of trial outcomes, particularly in small and complex trials that uses multi-component endpoints, such as PCOMs.

- **Further Research:** Extension to mixed endpoint types, as often in PCOMs, and more general statistical models.



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## Biased Patient Responses

$$X_j \sim \mathbf{N}_m(\mu_E t_j + \mu_C(1 - t_j) + \tau_j, \Sigma), \quad j \in \{1, \dots, N\}$$

- $N$ : Total sample size
- $m$ : The number of endpoint components
- $t_j = 1$  if patient  $j$  is allocated to treatment group ( $E$ ), and  $t_j = 0$  if allocated to control group ( $C$ )
- $\mu_i \in \mathbb{R}^m$ : Expected response vector for treatment  $i \in \{E, C\}$
- $\tau_j \in \mathbb{R}^m$ : Allocation bias effect for patient  $j$
- $\Sigma$ : covariance matrix

